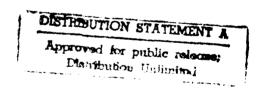
Computerized Inspection of Real Surfaces and Minimization of Their Deviations AD-A240 066

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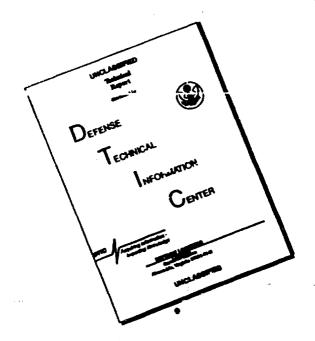
Prepared for the 5th International Conference on Metrology and Properties of Engineering Surfaces Leicester Polytechnic, England, April 10–12, 1991



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COMPUTERIZED INSPECTION OF REAL SURFACES AND MINIMIZATION OF THEIR DEVIATIONS

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SUMMARY

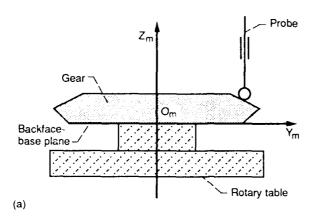
A method is developed for the minimization of gear tooth surface deviations between theoretical and real surfaces to improve the precision of surface manufacture. Coordinate measurement machinery is used to determine a grid of surface coordinates. Theoretical calculations are made for the grid points. A least-square method is used to minimize the deviations between real and theoretical surfaces by altering the manufacturing machine-tool settings. An example is given for a hypoid gear.

INTRODUCTION

The Gleason Works were pioneers in the application of coordinate measurements to improve the precision manufacturing of hypoid and spiral bevel gears (ref. 1). In aerospace applications, duplication of flight-qualified master gears is very important, and coordinate measurement has now become part of the normal production process. Methods to enhance and extend the use of this machinery can be very valuable to aerospace gear manufacturers.

The approach developed in this paper enables one do determine deviations of a real surface from the known theoretical surface. This is accomplished by using coordinate measurements and minimizing the deviations to correct the previously applied machine-tool settings. The surface deviations are represented in the direction of the normal to the theoretical surface. The coordinate measurements are performed by a machine with 4 or 5 degrees of freedom. In the case of 4 degrees of freedom, the probe performs three translational motions (fig. 1); the fourth motion, rotation, is performed by turning the table with the workpiece. The axis of rotational motion coincides with the axis of the workpiece. In the case of a 5-degree-of-freedom machine, the fifth degree of freedom is used to provide the probe deflections in the direction of the normal to the theoretical surface. The probe is provided with a changeable spherical surface whose diameter can be chosen from a wide range.

The motions of the probe and the workpiece for coordinate measurements are computer controlled and for this purpose a grid, the set of points on the surface to be measured, must be chosen. There is a reference point, one point on the grid, that is necessary for the initial installments of the probe. There are two orientations of the probe installment that are applied for measurements of a gear (fig. 1(a)) and a pinion (fig. 1(b)), depending on the angle I the pitch cone.



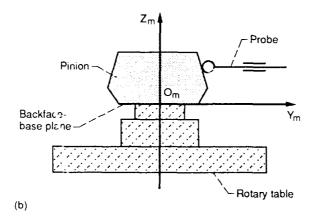


Figure 1.—Surface measurement orientation for (a) gear and (b) pinion.

The mathematical aspects of coordinate measurements will now be described (ref. 2): First, it is necessary to derive the equations for the theoretical surface. In many cases, this surface can be derived as the envelope to the family of generating surfaces, namely the tool surfaces. Next, the results of coordinate measurements must be transformed into deviations of the real surface represented in the direction of the surface normal. Here, the surface variations are represented in terms of the corrections to the machine-tool settings. The surface deviations obtained from coordinate measurements and the surface variations determined by the corrections of machine-tool settings can be represented by an overdetermined system of linear equations. The number k of these equations is equal to the number of grid points, and the number of unknowns m is equal to the number of corrections of machine-tool settings (m << k). The optimal solution to such a system of linear equations enables one to determine the sought-for corrections of machine-tool settings.

equations of theoretical tooth surface $\Sigma_{_{\rm t}}$

Considering that the theoretical surface can be determined directly, we represent it in coordinate system S_{\pm} in two-parametric form as

$$\mathbf{r}_{t}(\mathbf{u}, \boldsymbol{\theta}), \quad \mathbf{n}_{t}(\mathbf{u}, \boldsymbol{\theta})$$
 (1)

where \mathbf{r}_{t} and \mathbf{n}_{t} are the position vector and unit normal to the surface, respectively, and (\mathbf{u}, θ) are the Gaussian coordinates (surface coordinates).

For the case when surface $\Sigma_{\rm t}$ is the envelope to the family of generating surface $\Sigma_{\rm c}$, we represent in $S_{\rm t}$ surface $\Sigma_{\rm t}$ and the unit normal ${\bf n}_{\rm t}$ to $\Sigma_{\rm t}$ as (ref. 3)

$$\mathbf{r}_{t} = [\mathbf{M}_{tc}]\mathbf{r}_{c}(\mathbf{u}_{c}, \boldsymbol{\theta}_{c}), \mathbf{f}(\mathbf{u}_{c}, \boldsymbol{\theta}_{c}, \boldsymbol{\phi}) = 0$$
 (2)

$$\mathbf{n}_{t} = [\mathbf{L}_{tc}] \mathbf{n}_{c}(\mathbf{u}_{c}, \boldsymbol{\theta}_{c}), \mathbf{f}(\mathbf{u}_{c}, \boldsymbol{\theta}_{c}, \boldsymbol{\phi}) = 0$$
(3)

where (u_c,θ_c) are the Gaussian coordinates of the generating surface Σ_c , and ϕ is the generalized parameter of motion in the process for generation. The equation of meshing is

$$f(\mathbf{x}_{\mathbf{c}}, \mathbf{\theta}_{\mathbf{c}}, \mathbf{\phi}) : \mathbf{x}^{(\mathbf{c})} \cdot \mathbf{v}^{(\mathbf{c}\mathbf{t})} = 0$$
 (4)

where N^(c) is the normal to Σ_c , and $\mathbf{v}^{(\mathrm{ct})}$ is the relative motion for a point of contact of Σ_c and Σ_t . Matrices [M_{tc}]_{4x4} and [L_{tc}]_{3x3} describe the coordinate transformation from S_c to S_t for a position vector and surface normal, respectively. Position vectors in three-dimensional space are represented with homogeneous coordinates.

COORDINATE SYSTEMS USED FOR COORDINATE MEASUREMENTS

Coordinate systems $S_{\rm m}$ and $S_{\rm t}$ are rigidly connected to the coordinate measuring machine (CMM) and the workpiece being measured, respectively (fig. 2). The

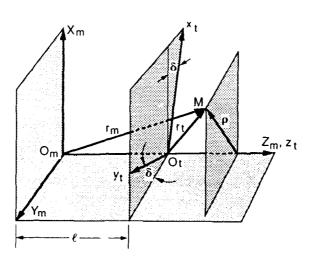


Figure 2.—Relationship between theoretical and measurement coordinate systems. (ρ , radial distance to point from axis of rotation.)



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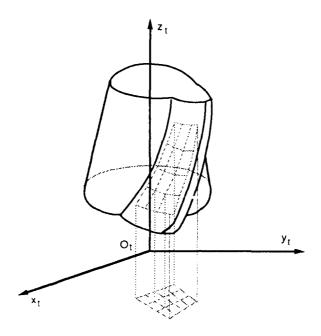


Figure 3.—Measurement grid on tooth surface.

backface of the gear is installed flush with the base plane of CMM. The distance 1 between the origins O_m and O_t is assumed to be known, but the parameter δ of orientation must be determined (see the following section). The coordinate transformation from S_t to S_m is represented by the matrix equation

$$\mathbf{r}_{m} = [\mathbf{M}_{mt}]\mathbf{r}_{t} \tag{5}$$

MEASUREMENT GRID AND ESTABLISHMENT OF THE REFERENCE POINT

The grid is a set of points on $\Sigma_{\rm t}$ chosen as points of contact between the probe and $\Sigma_{\rm t}$ (fig. 3). Fixing the value of $z_{\rm t}$ for the point of the grid and the value of, say, $\gamma_{\rm t}$ (or $x_{\rm t}$), we can obtain the following equations:

$$y_t(u_i, \theta_i) = h_i, z_t(u_i, \theta_i) = l_i (i = 1, ..., k)$$
 (6)

where k is the number of grid points.

We consider h_i and l_i as given and solve equations (6) for (u_i, θ_i) . Then we can determine the position vectors and the unit normals for k points of the grid using the equations

$$\mathbf{r}_{+}^{(i)} = [\mathbf{x}_{t}(\mathbf{u}_{i}, \theta_{i}) \mathbf{y}_{t}(\mathbf{u}_{i}, \theta_{i}) \mathbf{z}_{t}(\mathbf{u}_{i} \theta_{i})]^{T}, \qquad (i = 1, ..., k)$$
 (7)

$$\mathbf{n}_{+}^{(i)} = [\mathbf{n}_{xt}(\mathbf{u}_{i}, \theta_{i}) \mathbf{n}_{vt}(\mathbf{u}_{i}, \theta_{i}) \mathbf{n}_{xt}(\mathbf{u}_{i}, \theta_{i})]^{T}, \qquad (i = 1, ..., k)$$
(8)

The position vector for the center of the probe, if the deviations are zero, is represented by

$$R_{+}^{(i)} = r_{+}^{(i)} + \rho n_{+}^{(i)}$$
 (i = 1,...,k) (9)

where ρ is the radius of the probe sphere.

The reference point

$$\mathbf{r}_{+}^{(o)} = \left[\mathbf{x}_{+}(\mathbf{u}^{(o)}, \boldsymbol{\theta}^{(o)}) \mathbf{y}_{+}(\mathbf{u}^{(o)}, \boldsymbol{\theta}^{(o)}) \mathbf{z}_{+}(\mathbf{u}^{(o)}) \right]^{T}$$
(10)

is usually chosen as the mean point of the grid.

The center of the probe that corresponds to the reference point on $\Sigma_{\rm t}$ is determined from equation (9) as

$$\mathbf{R}_{t}^{(\circ)} = \left[\mathbf{X}_{t}(\mathbf{u}^{(\circ)}, \boldsymbol{\theta}^{(\circ)}) \mathbf{Y}_{t}(\mathbf{u}^{(\circ)}, \boldsymbol{\theta}^{(\circ)}) \mathbf{Z}_{t}(\mathbf{u}^{(\circ)}, \boldsymbol{\theta}^{(\circ)}) \right]^{\mathrm{T}}$$
(11)

where $(u^{(o)}, \theta^{(o)})$ are known values.

The coordinates of the reference center of the probe are represented in coordinate system S_{m} of the measuring machine by the matrix equation

$$\mathbf{R}_{m}^{(0)} = \left[\mathbf{M}_{mt}(\delta)\right] \mathbf{R}_{+}^{(0)} \tag{12}$$

Equation (12) yields

$$x_{m}^{(o)} = x_{m}^{(o)} (\delta, u^{(o)}, \theta^{(o)})$$

$$y_{m}^{(o)} = y_{m}^{(o)} (\delta, u^{(o)}, \theta^{(o)})$$

$$z_{m}^{(o)} = z_{m}^{(o)} (\delta, u^{(o)}, \theta^{(o)})$$
(13)

Three equations (13) contain four unknowns: δ , $x_m^{(o)}$, $y_m^{(o)}$, $z_m^{(o)}$. To solve these equations, we may consider that one of the coordinates of the reference point of the

probe center, say, $y_m^{(o)}$, may be chosen equal to zero. This is accomplished by requiring the reference point to lie in the $x_m - z_m$ plane. The orientation of angle δ is now established to satisfy this requirement, and all measurements are referenced from this location. Then equation system (13) allows one to determine

 δ , $x_m^{(\circ)}$ and $z_m^{(\circ)}$ (ref. 2). Coordinates $x_m^{(\circ)}$, $y_m^{(\circ)}$ = 0, $z_m^{(\circ)}$ are necessary for the initial installment of the center of the probe.

MEASUREMENT OF THE DEVIATIONS OF THE REAL SURFACE

The deviations of the real surface are caused by manufacturing errors, heat treatment, etc. Vector positions of the center of the probe for the theoretical surface and the real surface can be represented as follows:

$$\mathbf{R}_{m} = \mathbf{r}_{m}(\mathbf{u}, \boldsymbol{\theta}) + \rho \mathbf{n}_{m}(\mathbf{u}, \boldsymbol{\theta}) \tag{14}$$

$$\mathbf{R}_{m}^{*} = \mathbf{r}_{m}(\mathbf{u}, \boldsymbol{\theta}) + \lambda \mathbf{n}_{m}(\mathbf{u}, \boldsymbol{\theta})$$
 (15)

where ${\bf r}_{\rm m}$ and ${\bf n}_{\rm m}$ are the position vector and the unit normal to the theoretical surface and are represented in coordinate system $S_{\rm m}$ of the measuring machine; λ determines the real location of the probe center and is considered along the normal

to the theoretical surface; $R_{\rm m}$ and $R_{\rm m}^*$ represent in $S_{\rm m}$ the position vector of the probe center for the theoretical and real surfaces, respectively. Equations (14) and (15) yield

$$\mathbf{R}_{\mathrm{m}}^{*} - \mathbf{R}_{\mathrm{m}} = (\lambda - \rho) \mathbf{n}_{\mathrm{m}} = \Delta n \mathbf{n}_{\mathrm{m}}$$
 (16)

and

$$\Delta n = (R_m^* - R_m) \cdot n_m \tag{17}$$

The position vector \mathbf{R}_{m}^{*} is determined by coordinate measurements for points of the grid. Equation (17) determines numerically the function

$$\Delta n_i = \Delta n_i(u_i, \theta_i) \qquad (i = 1, ..., k)$$
 (18)

that represents the deviations of the real surface for each point of the grid.

MACHINE TOOL SETTINGS TO MINIMIZE DEVIATIONS

The procedure used to minimize the deviations can be represented in two stages: (1) determination of variations of theoretical surface caused by changes of applied machine-tool settings, and (2) minimization of deviations of real surface by appropriate correction of machine-tool settings.

We consider that the theoretical surface is represented in $S_{_{+}}$ as

$$\mathbf{r}_{t} = \mathbf{r}_{t}(\mathbf{u}, \theta, \mathbf{d}_{j}) \qquad (j = 1, \dots, m)$$
 (19)

where parameters d are the machine-tool settings. The surface variation is represented by

$$\delta \mathbf{r}_{t} = \frac{\partial \mathbf{r}_{t}}{\partial \mathbf{u}} \delta \mathbf{u} + \frac{\partial \mathbf{r}_{t}}{\partial \theta} \delta \theta + \sum_{j=1}^{m} \frac{\partial \mathbf{r}_{t}}{\partial \mathbf{d}_{j}} \delta \mathbf{d}_{j}$$
 (20)

We multiply both sides of equation (20) by the surface unit normal \mathbf{n}_t and take into account that $\partial \mathbf{r}_t/\partial \theta + \mathbf{n}_t = \partial \mathbf{r}_t/\partial \mathbf{u} + \mathbf{n}_t = 0$, since $\partial \mathbf{r}_t/\partial \theta$ and $\partial \mathbf{r}_t/\partial \mathbf{u}$ lie in the plane that is tangent to the surface. Then we obtain

$$\delta \mathbf{r}_{t} \cdot \mathbf{n}_{t} = \sum_{j=1}^{m} \left(\frac{\partial \mathbf{r}_{t}}{\partial \mathbf{d}_{j}} \cdot \mathbf{n}_{t} \right) \delta \mathbf{d}_{j} = \sum_{j=1}^{m} a \delta \mathbf{d}_{j}$$
(21)

We can now consider a system of $\,k\,$ linear equations in $\,m\,$ unknowns $\,(m\,<<\,k)$ of the following structure:

Here

$$b_{i} = \Lambda n_{i} = (R_{mi}^{*} - R_{mi}) \cdot n_{mi}$$
 (23)

where i designates the number of grid points; a $(s=1,\ldots,k;\ j=1,\ldots,m)$ represents the dot product of partial derivatives $\partial \mathbf{r}_t/\partial \mathbf{d}_j$ and unit normal \mathbf{n}_t . The system (22) of linear equations is overdetermined since m << k. The essence of the procedure for minimization of deviations is determining unknowns $\partial \mathbf{d}_j$ (j = 1,...,m) that will minimize the difference between the left and right sides of equations (22). The solution employed the least-square method. The subroutine DLSQRR of IMSL MATH/LIBRARY (ref. 4) was used to computerize the procedure.

APPLICATION OF METHOD TO THE INSPECTION OF FORMATE HYPOID GEAR

Each tooth side of a formate face-hobbed gear is generated by a cone, and the gear tooth surface is the surface of the generating cone. Two cones that are shown in figure 4(a) represent both sides of the gear space. The following equations represent in coordinate system $S_{\rm c}$ gear surfaces for both sides and the unit normal to such surfaces (fig. 4(b)):

$$\mathbf{r}_{c} = \begin{bmatrix} -s_{g}\cos\alpha_{g} \\ (r - s_{g}\sin\alpha_{g})\sin\theta_{g} \\ (r - s_{g}\sin\alpha_{g})\cos\theta_{g} \end{bmatrix}$$
(24)

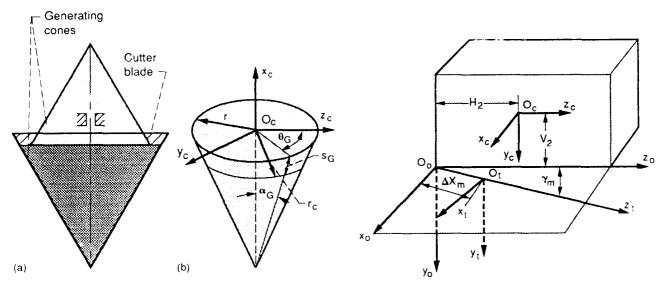


Figure 4 —Generating cones representing cutter blades

Figure 5.—Coordinate system orientation and machine-tool settings for hypoid gear.

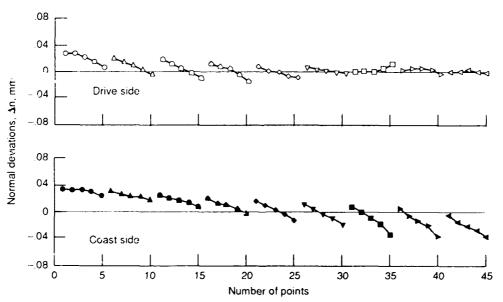


Figure 6.—Deviations of gear real tooth surface.

$$\mathbf{n}_{c} = \begin{bmatrix} \sin \alpha_{g} \\ -\cos \alpha_{g} \sin \theta_{g} \\ -\cos \alpha_{g} \cos \theta_{g} \end{bmatrix}$$
 (25)

where, \mathbf{r}_{g} is the position vector and \mathbf{n}_{g} the unit normal; \mathbf{r}_{g} is the cutter blade angle (α_{g}^{c} > 0 for the concave side and α_{g} < 0 for the convex side).

Figure 5 shows the installment of the generating cone on the cutting machine. Coordinate systems S_{i} and S_{t} are rigidly connected to the cutting machine and the gear being generated, respectively. Systems S_{i} , S_{i} , and S_{t} are rigidly connected to each other since the gear is formate cut. To represent in S_{t} the theoretical gear tooth surface S_{t} and the unit normal to S_{t} , we use the following matrix equations:

$$\mathbf{r}_{t}(\mathbf{s}_{G}, \boldsymbol{\theta}_{G}, \mathbf{d}_{t}) = [\mathbf{M}_{tc}]\mathbf{r}_{c}(\mathbf{s}_{G}, \boldsymbol{\theta}_{G})$$
 (26)

$$\mathbf{n}_{\mathsf{t}}(\mathbf{s}_{\mathsf{g}}, \boldsymbol{\theta}_{\mathsf{g}}, \mathbf{d}_{\mathsf{j}}) = [\mathbf{L}_{\mathsf{tc}}] \mathbf{n}_{\mathsf{c}}(\mathbf{s}_{\mathsf{g}}, \boldsymbol{\theta}_{\mathsf{g}}) \tag{27}$$

where

$$\begin{bmatrix} \mathbf{M}_{\text{to}} \end{bmatrix} = \begin{bmatrix} \mathbf{M}_{\text{to}} \end{bmatrix} \begin{bmatrix} \mathbf{M}_{\text{oc}} \end{bmatrix}$$

$$= \begin{bmatrix} \cos \gamma_{\text{m}} & 0 & -\sin \gamma_{\text{m}} & 0 \\ 0 & 1 & 0 & 0 \\ \sin \gamma_{\text{m}} & 0 & \cos \gamma_{\text{m}} & -\Delta x_{\text{m}} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -v_{2} \\ 0 & 0 & 1 & H_{2} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$(28)$$

The surface Gaussian coordinates are s $_{\rm g}$ and $\theta_{\rm g}$, and d $_{\rm j}(\gamma_{\rm m},~{\rm V_2},~{\rm H_2},~{\rm and}~\Delta{\rm X_m})$ are the machine-tool settings.

The numerical example presented in this paper is based on the experiment that has been performed at the Dana Corporation (Fort Wayne, IN, U.S.A.). The initial deviations Δn for each side of the real tooth surface have been obtained by measurements on a coordinate measuring machine (fig. 6). The grid for the measurement is formed by nine sections along the tooth length, each section having five points. The number of grid points k is therefore 45, and the reference point is at the middle of the grid, i.e., the third point of the fifth section. In the measure-

ment, the coordinate $y_m^{(o)}$ of the reference point is chosen to be zero and the alignment angle δ is determined from solving equation system (13).

The minimization of deviations was performed in accordance with the algorithm described in MACHINE TOOL SETINGS TO MINIMIZE DEVIATIONS, and the results are illustrated in figure 7 and table I.

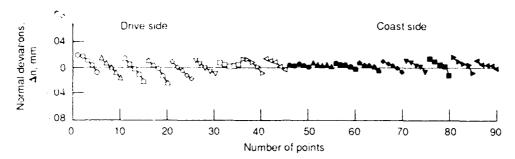


Figure 7 -- Minimized deviations after corrections made to machine-tool settings

TABLE I. - RESULTS OF MINIMIZATION

[Pressure angle, $\alpha_{\gamma} = 21.25^{\circ}$; cutter diameters = 9 in.; point width of cutters = 0.08 in.]

| Machine-tool settings | Machine-too1 setting parameters | | | | |
|--------------------------|---------------------------------|------------------------|------------------------------|----------------------|--|
| | V ₂ , mm | H ₂ , mm | $\gamma_{\mathfrak{m}'}$ rad | $\Delta x_{_{m}}$, | |
| Initial Corrected | 103.252550 103.25220 | 27.466600 27.21603 | 1.059816 1.06437 | 0.009677 -0.53343 | |

CONCLUSION

A general approach for a computerized determination of deviations of a real surface from the theoretical one based on coordinate measurements has been proposed. An algorithm for computerized minimization of deviations by corrections of initially applied machine-tool settings has been developed. The approach is illustrated with the example of the tooth surface of a hypoid formate gear.

ACKNOWLEDGMENT

This research has received financial support from the NASA Lewis Research Center, Gleason Memorial Fund, and the Dana Corporation.

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| 1. Report No. NASA TM - 103798 AVSCOM TR 91 - C - 0 | 2. Government Accession | n No. | Recipient's Catalog N | o. | | | |
| 4. Title and Subtitle Computerized Inspection of Real S of Their Deviations | | 5. Report Date | | | | | |
| | | | 6. Performing Organizat | ion Code | | | |
| 7 Author(s) F.L. Litvin, Y. Zhang, C. Kuan, an | | 8. Performing Organizat E =6086 | ion Report No | | | | |
| | | | 10. Work Unit No. | | | | |
| 9 Performing Organization Name and Address NASA Lewis Research Center Cleveland, Ohio. 44135 - 3191 | | 505 -63-36 1L162 A47A | | | | | |
| and Propulsion Directorate | | | 11. Contract or Grant No | | | | |
| U.S. Army Aviation Systems Com Cleveland, Ohio 44135 - 3191 | mand | | 13. Type of Report and P | eriod Covered | | | |
| 12 Sponsoring Agency Name and Address National Aeronautics and Space Ad- Washington, D.C. 20546 - 0001 | | Technical Memo | | | | | |
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| 15 Supplementary Notes Prepared for the 5th International C England, April 10-12, 1991. F.L. Chicago, Chicago, Illinois 60680 (ate, U.S. Army Aviation Systems C | Litvin, Y. Zhang, C. Kuar (work funded under NAS) | i, Dept. of Mechanic A Grant NAG3-964 | cal Engineering, Univ | ersity of Illinois at | | | |
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| 17 Key Words (Suggested by Author(s)) | | 18. Distribution Stateme | | | | | |
| Gears Gear t eth Mechanical drives Coordinate transformations | | Unclassified - Unlimited Subject Category 37 | | | | | |
| 19 Security Classif. (of the report) | 20. Security Classif. (of | , , , | 21. No. of pages | 22. Price* | | | |
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